

APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY
FIRST SEMESTER M.TECH DEGREE EXAMINATION
Computer Science and Engineering
(Computer Science and Systems Engineering)
04 CS 6405 - Automata Theory and Computability

Time: 3 hrs

Max. Marks: 60

PART A

(Answer all questions. Each question carry 3 marks).

1. Design a DFA over $\{a, /, *\}$ which end in a C-Style comment. (3)
2. Give a regular expression for the language $L = \{w \in (a, b)^*\}$ such that no two a's and no two b's come together in w. (3)
3. Give the language represented by the regular expression. (3)

$$1(0 + 1)^* + (1 + 0)^*0$$

4. What is Ultimately Periodic Set? (3)
5. What is the language represented by the following Context Free Grammar? (3)

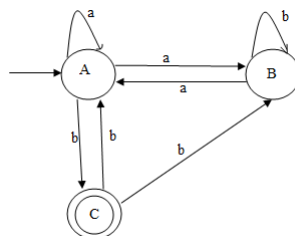
$$S \rightarrow aSb / bSa / \epsilon$$

6. What are Null Productions? What is their effect on deciding whether a given string is present in a given language or not of Context Free Language? (3)
7. How the Universal Turing Machine works? (3)
8. Let T be a Turing Machine, give the formal definition of T. (3)

PART B

(Each full question carries 6 marks).

9. Convert the following NFA into its equivalent DFA. (6)



OR

10. Design an NFA for the language over $(0,1)$ with set of all strings that end with 01 and convert it into equivalent DFA. (6)

11. Convert the given CFG to CNF. (6)

$$S \rightarrow aSb/bSa/\epsilon$$

OR

12. Obtain a reduced grammar equivalent to the grammar G having the productions. (Remove useless, null and unit productions) (6)

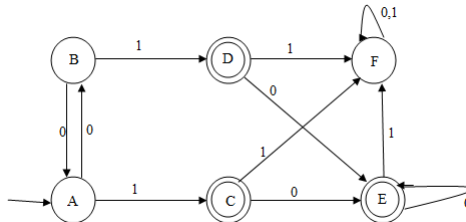
$$S \rightarrow AC/B$$

$$A \rightarrow a$$

$$C \rightarrow c/BC$$

$$E \rightarrow aA/e$$

13. Obtain the unique minimal DFA corresponding to the canonical Myhill Nerode relation representing the language by the following DFA. (6)



OR

14. Prove that the language $L = \{a^n b^n | n > 0\}$ is not regular using Pumping Lemma. (6)

15. Give a PDA (accepts by final state) accepting the language $L = \{a^n b^n c^m | n, m \geq 1\}$. (It is enough to give the set of transitions or the transition graph). (6)

OR

16. Give a PDA (accepts by final state) accepting the language $L = \{a^n b^{2n} | n \geq 1\}$. (It is enough to give the set of transitions or the transition graph). (6)

17. Design a Turing Machine to recognise the language $L = \{w \Pi w\}$ where the first half is repeated in the second half and Π is the separation between them. (It is enough to give the set of transitions or the transition graph). (6)

OR

18. Design a Turing Machine to recognise the language $L = \{a^n b^n c^n | n \geq 0\}$. (It is enough to give the set of transitions or the transition graph). (6)

19. State and prove Rice's Second Theorem. (6)

OR

20. State and prove the theorem which shows M such that M accepts an infinite language is undecidable. (6)