

APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY

Scheme for Valuation/Answer Key

Scheme of evaluation (marks in brackets) and answers of problems/key

EIGHTH SEMESTER B.TECH DEGREE EXAMINATION, MAY 2019

Course Code: CE466

Course Name: FINITE ELEMENT METHODS

Max. Marks: 100

Duration: 3 Hours

PART A

Answer any two full questions, each carries 15 marks.

- | | Marks |
|--|-------|
| 1 a) 1. element type (1) | (10) |
| 2. Select displacement model and shape functions(2) | |
| 3. Strain -displacement relation(1) | |
| 4. Element Stiffness matrix(1) | |
| 5. Assembly of elements(1) | |
| 6. Boundary conditions(1) | |
| 7. Solution of equilibrium equation for displacements(1) | |
| 8. Stress computations and reactions(2) | |
| b) 1. continuous | (5) |
| 2. interelement continuity | |
| 3. rigid body displacement | |
| 4. Constant strain state | |
| 5. Monotonic convergence, complete | |
| 2 a) State principle(2), example of simple bar element- Internal strain energy(1), | (5) |
| external strain energy(1), Total SE minimization with derivative =0 (1) | |
| b) $Ax=B$ form (1), forward elimination(2), backward elimination(2) | (5) |
| c) Potential π | (3) |
| $u=a_1x$ | (1) |
| Stress = $qL^2/3A$ | (1) |
| 3 a) 1) Collocation method | (2) |
| 2) Galerkin method with 2 terms, $U=a_1x+a_2x^2$ | (2) |
| Stress = $cL/2AE x - c/6AE x^3$ | |
| 3) Least squares method | (2) |
| b) Definition of shape functions | (1.5) |

Properties (2x3)	(6)
Significance	(1.5)

PART B

Answer any two full questions, each carries 15 marks.

- 4 a) Element stiffness matrix – (1 x 3 = 3 marks) (10)
 Global stiffness matrix - (2 marks)
 Boundary conditions - (1 marks)
 Equilibrium equations – (1 mark)
 Solution to obtain nodal displacements - (1 marks)
 Forces in each element - (1 mark)
 Reactions - (1 mark)
- b) Static condensation – need for condensation (2 marks) (5)
 Method for condensation - (3 marks)
- 5 a) Element stiffness matrix – (1.5 x 2 = 3 marks) (10)
 Global stiffness matrix - (1 mark)
 Boundary conditions - (2 marks)
 Equilibrium equations – (1 mark)
 Solution to obtain nodal displacements - (2 marks)
 Reactions – (1 mark)
- b) Displacement boundary conditions – (2 marks) (5)
 Equilibrium equations in terms of restrained and unrestrained displacements – (3 marks)
- 6 a) 2-noded beam element using Hermitian interpolation (5)
 3-noded bar using Lagrangian interpolation (5)
- b) C^0 definition, example bar/truss element (2)
 C^1 definition, example beam element (2)
 Trigonometric functions can model both C^0 and C^1 elements (1)

PART C

Answer any two full questions, each carries 20 marks.

- 7 a) Lagrange Interpolation functions (2)
 (8)

- Derivation of shape functions at four nodes
- b) Constant strain (2.5)
 Linear strain (2.5)
- c) Isoparametric relation- shape functions of quadrilateral element (2)
 Substituting (0.6,.8) and finding shape functions (1)
 $X=N_1x_1+N_2x_2+N_3x_3+N_4x_4$ and for y (1)
 Substituting and finding values $x=5.82, y=7.02$ (1)
- 8 a) 2-point Gauss quadrature, weights and gauss points (6)
 Result (2)
 Exact solution comparison (2)
- b) Kirchoff plate bending theory (2.5)
 Mindlin plate bending theory (2.5)
- c) Patch test description (4)
 Importance (1)
- 9 a) Definition (1)
 Expression for consistent nodal load (2)
 shape function matrix along the edge where surface load acts (2)
 shape functions (3)
 surface load vector along the corresponding edge (2)
- b) 1. element type (1) (10)
 2. Geometry mapping using isoparametric mapping(3)
 3.Select displacement model and same shape functions(2)
 4.Strain -displacement relation(2)
 5.Element Stiffness matrix(2)
