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APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY
FIFTH SEMESTER B.TECH DEGREE EXAMINATION(R&S), DECEMBER 2019

Course Code: EC301

Course Name: DIGITAL SIGNAL PROCESSING

Max. Marks: 100

Duration: 3 Hours

PART A

Answer any two full questions, each carries 15 marks.

Marks

- 1 a) State Parseval's theorem of DFT? Using DFT find the energy of the sequence $x(n) = 0.2^n u(n), n < 4$. (7)
- b) Compute 8-point DFT of the sequence $x(n) = \{\frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, 0, 0, 0, 0\}$ using DITFFT algorithm. Follow exactly the corresponding flow graphs and keep track of all the intermediate quantities by putting them on diagram. (8)
- 2 a) Find linear convolution of the sequences $x(n)$ and $z(n)$ using circular convolution. Given $x(n) = \{1, 2, 3, 1\}$ and $z(n) = \{4, 3, 2\}$. (7)
- b) Explain how N point DFTs of two real sequences can be found using by computing a single DFT. Illustrate with the sequences $x_1(n) = \{4, 3, -1, 5\}$ and $x_2(n) = \{6, -4, 2, 5\}$. (8)
- 3 a) Find the number of real multiplications and additions involved in the computation of 64-point DFT using i) direct computation ii) FFT algorithm. Also comment on the computational advantage of FFT algorithm over the direct method. (7)
- b) Using Overlap Add method, find the output of the filter with filter response $h(n)$ when an input $x(n) = \{1, 2, 2, 3, 4, 2, 2, 1, 1\}$ is given. Take data block size of length $L = 3$ and $h(n) = \{2, 3, 4\}$. (8)

PART B

Answer any two full questions, each carries 15 marks.

- 4 a) Design a linear phase FIR low pass filter with cut off frequency of 2 kHz and sampling rate of 8 kHz with a filter length 11 using Hanning window. (10)
- b) Find the filter transfer function $H(z)$ from the analog filter with system function $H(s)$ using Impulse Invariance method. (5)

$$H(s) = \frac{s + 1}{s^2 + 0.2s + 16.01}$$

- 5 a) Apply frequency sampling technique to design a linear phase FIR filter of length $N=7$ with following specification. (10)

$$H_d(e^{j\omega}) = \begin{cases} e^{-j\alpha\omega}; & 0 \leq |\omega| \leq 0.55\pi \\ 0 & \text{otherwise} \end{cases}$$

- b) Transform the prototype low pass filter with system function $H(s) = \frac{\Omega_c}{s + \Omega_c}$ (5)
into high pass and band pass filters.
- 6 a) Design a Butterworth low pass digital IIR filter with a pass band edge frequency of 0.25π with a ripple not exceeding **0.5 dB** and a minimum stop band attenuation **15dB** with a stop band edge frequency of 0.55π . Use bilinear transformation. (10)
- b) Compare the performance of FIR filter design using rectangular window and Hamming window. (5)

PART C

Answer any two full questions, each carries 20 marks.

- 7 a) Determine a direct form realization of the FIR filter with the following filter function using minimum number of multipliers. (4)
 $h(n) = \{1, 2, 3, 4, 3, 2, 1\}$
- b) Draw the cascade and parallel form realisation of the filter with following transfer function (8)

$$H(z) = \frac{3(5 - 2z^{-1})}{\left(1 + \frac{1}{2}z^{-1}\right)(3 - z^{-1})}$$

- c) How upsampling and downsampling by a factor of 3 affect the frequency spectrum of a signal $x(n)$ with frequency spectrum $X(e^{j\omega})$? What is the need of low pass filter prior to downsampling? (8)
- 8 a) For the signal $x(n) = 0.2^n u(n), n \leq 8$, plot the following signals (4)
(i) $x(n)$ downsampled by 3 (ii) $x(n)$ upsampled by 3
- b) With an example illustrate the error introduced by truncation and rounding in fixed point representation of numbers. (8)
- c) What is the effect of coefficient quantization in IIR filter structures? (8)
- 9 a) Obtain the direct form II, cascade and transposed direct form II structures for the (10)

system.

$$y(n) = -0.1y(n-1) + 0.2y(n-2) + 3x(n) + 3.6x(n-1) + 0.6x(n-2)$$

- b) Explain the architecture of TMS320C67xx DSP with block diagram. (10)
