

Reg No.: \_\_\_\_\_

Name: \_\_\_\_\_

**APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY**  
**FIFTH SEMESTER B.TECH DEGREE EXAMINATION(R&S), DECEMBER 2019**

**Course Code: AE301**

**Course Name: CONTROL SYSTEM**

Max. Marks: 100

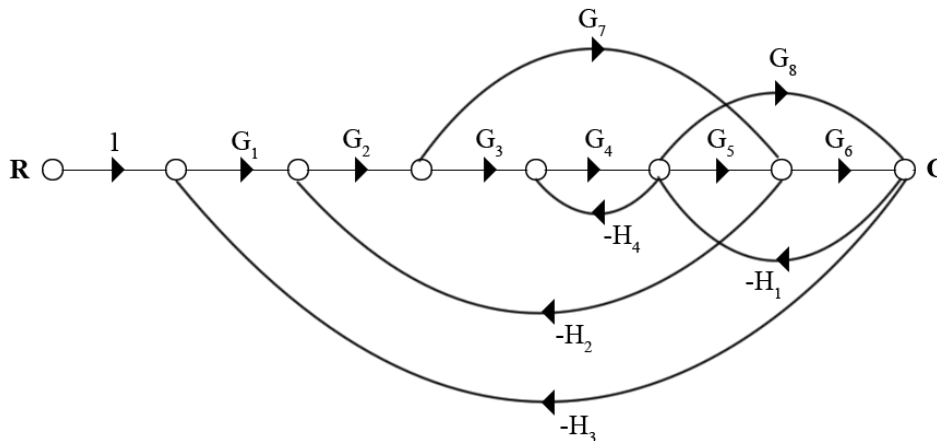
Duration: 3 Hours

*Provide one graph sheet and one semi-log sheet.*

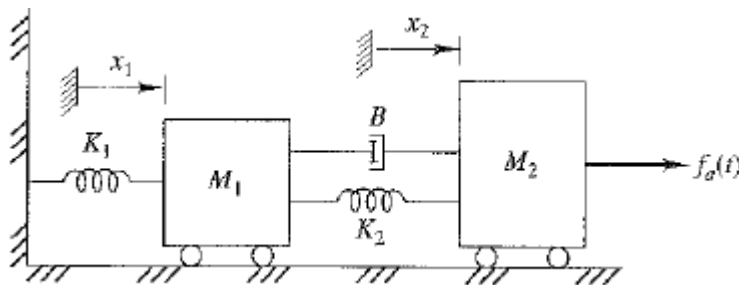
**PART A**

*Answer any two full questions, each carries 15 marks.*

- |   |   |       |
|---|---|-------|
| 1 | <ul style="list-style-type: none"> <li>a) Explain Mason's Gain formula. <span style="float: right;">(3)</span></li> <li>b) Differentiate Open-Loop Control Systems and Closed-Loop Control Systems with examples. <span style="float: right;">(4)</span></li> <li>c) Obtain the overall transfer function from the signal flow graph shown in figure. <span style="float: right;">(8)</span></li> </ul> | Marks |
|---|---|-------|



- |   |   |       |
|---|---|-------|
| 2 | <ul style="list-style-type: none"> <li>a) What is order and type of a system? <span style="float: right;">(2)</span></li> <li>b) Obtain the differential equations of mechanical system shown in figure and find transfer function of the system. <span style="float: right;">(8)</span></li> </ul> | Marks |
|---|---|-------|



- |    |   |  |
|----|---|--|
| c) | Derive an expression for steady state error of a unity negative feedback system. <span style="float: right;">(5)</span> |  |
|----|---|--|

- 3 a) For a unity feedback control system, the open loop transfer function (4)

$$G(s) = \frac{10(s + 2)}{s^2(s + 1)}$$

Find the position, velocity and acceleration error constants.

- b) Obtain the response of unity feedback system whose open loop transfer function is (6)

$$G(s) = \frac{4}{s(s + 5)}$$

and when the input is unit step.

- c) Derive the expression for  $c(t)$ , the time response of an undamped second order control system. (5)

### PART B

*Answer any two full questions, each carries 15 marks.*

- 4 a) Explain BIBO stability. (2)
- b) Explain Routh Hurwitz Criterion. (4)
- c) Construct Routh array and determine the stability of the system whose characteristic equation is  $s^6 + 2s^5 + 8s^4 + 12s^3 + 20s^2 + 16s + 16 = 0$ . Also determine the number of roots lying on right half of  $s$  plane, left half of  $s$  plane and on imaginary axis. (9)
- 5 a) Explain frequency domain specifications. (5)
- b) Sketch the root locus of a unity feedback system whose open-loop transfer function is (10)

$$G(s) = \frac{K(s+9)}{s(s^2+4s+11)}$$

- 6 a) The open loop transfer function of a system is (5)

$$G(s) = \frac{K}{s(1 + 0.1s)(1 + s)}$$

Determine the value of  $K$  so that the gain margin is 6dB.

- b) Plot the Bode diagram for the following transfer function. (8)

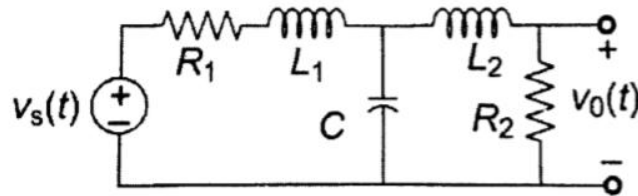
$$G(s) = \frac{10}{s(1 + 0.4s)(1 + 0.1s)}$$

- c) Explain the concept of encircled and enclosed. (2)

## PART C

Answer any two full questions, each carries 20 marks.

- 7 a) What are the drawbacks of transfer function model analysis? (4)  
 b) Define the following terms: i) State ii) State Vector iii) State variables (6)  
 c) Obtain the state model of the electrical network shown in figure. (10)



- 8 a) Consider the matrix  $A = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix}$ . Compute the state transition matrix by Laplace transform method. (8)  
 b) Obtain the state model of the system whose transfer function is (8)  

$$\frac{Y(s)}{U(s)} = \frac{10}{s^3 + 4s^2 + 2s + 1}$$
  
 c) Explain Bush form or Companion Form. (4)
- 9 a) Determine the controllability and observability of the system  $\dot{X} = AX + BU$  where (10)  
 $Y = CX$

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \end{bmatrix} = \begin{bmatrix} 2 & -2 & 3 \\ 1 & 1 & 1 \\ 1 & 3 & -1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} 11 \\ 1 \\ -14 \end{bmatrix} u$$

$$y = [-3 \quad 5 \quad -2] \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}$$

- b) Obtain the state transition matrix  $\Phi(t)$  of the following system (7)

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$

Obtain the inverse of the state transition matrix.

- c) Define Controllability of LTI system. (3)

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