



Course Code: CE203

Course Name: FLUID MECHANICS -I

Max. Marks: 100

Duration: 3 Hours

Scheme of evaluation

**PART A**

1. a)  $p = \gamma h$  ..... 1 mark  
 $p = 350 \text{ kN/m}^2$   
 For water,  $\gamma = 9.810 \text{ kN/m}^3$ ,  $\therefore h = 35.68 \text{ m}$  ..... 1 mark  
 For mercury,  $\gamma = 13.6 \times 9.810 \text{ kN/m}^3$ ,  $\therefore h = 2.62 \text{ m}$  ..... 1 mark  
 $p_{\text{absolute}} = p + p_{\text{atmosphere}}$  ..... 1 mark  
 $= 350 + 101.3 = 451.3 \text{ kN/m}^2$  ..... 1 mark

**Total -5 marks**

- b) Figure ..... 1 mark

$F = \gamma A \bar{x}$  ..... 1 mark

$\bar{x} = 1.75 \text{ m}$ ,  $\gamma = 0.9 \times 9810$ ,

$A = \frac{\pi}{4} (1.5^2 - 1^2) = 0.981 \text{ m}^2$  .... 1 mark

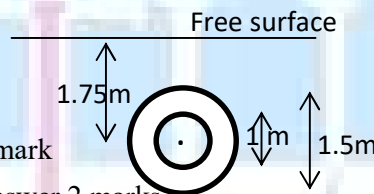
$F = 15.16 \text{ kN}$ ..... Substitution & answer 2 marks

$\bar{h} = \bar{x} + \frac{I_g}{A \bar{x}}$  ..... 2 marks

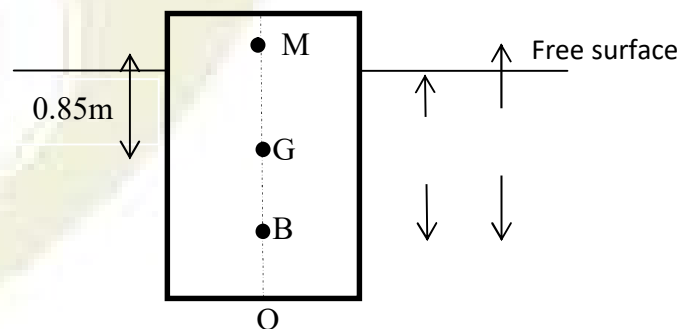
$I_g = \frac{\pi}{64} (1.5^4 - 1^4) = 0.1993 \text{ m}^4$  ..... 1 mark

$\bar{h} = 1.866 \text{ m}$  .... Substitution & answer 2 marks

**Total -10 marks**



2. (a)  $\overline{GM} = \frac{wx}{W \tan \theta}$  ..... 1 mark  
 $W = 15000 \text{ kN}$ ,  $w = 200 \text{ kN}$ ,  $x = 5 \text{ m}$ ,  $\theta = 4.5^\circ$   
 $\overline{GM} = 0.85 \text{ m}$  ..... 2 marks  
 $\overline{BM} = \frac{I}{V}$  ..... 1 mark  
 $I = 0.8 \times \frac{60 \times 10^3}{12} = 4000 \text{ m}^4$  ..... 2 marks  
 $V = \frac{15000}{9.81 \times 1.03} = 1484.5 \text{ m}^3$  ..... 1 mark  
 $\overline{BM} = 2.695 \text{ m}$  ..... 1 mark  
 $\overline{GB} = 1.845 \text{ m}$  ..... 1 mark  
 Depth of G below water surface = 0.155 m ..... 1 mark



**Total -10 marks**

- (b) proof ..... 5 marks

3. (a) Eulerian and Lagrangian methods..... 1.5 marks each

**Total - 3 marks**

(b)  $v = \frac{\partial \psi}{\partial x} = 2y$ .....1 mark

$u = -\frac{\partial \psi}{\partial y} = -2x$ .....1 mark

$\frac{\partial u}{\partial x} = -2$ .....0.5 mark

$\frac{\partial v}{\partial y} = 2$ .....0.5 mark

$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0$ . So flow exists.....1 mark

$\frac{\partial^2 \psi}{\partial x^2} = 0$ .....1 mark

$\frac{\partial^2 \psi}{\partial y^2} = 0$ .....1 mark

$\frac{\partial^2 \psi}{\partial x^2} + \frac{\partial^2 \psi}{\partial y^2} = 0$ . Therefore flow is irrotational. ....1 mark

**Total - 7 marks**

- (c) (i) steady flow and unsteady flow. ....2.5 marks

- (ii) uniform flow and Non uniform flow. ....2.5 marks

**Total - 5 marks**

**PART B**

4. (a) Sketch-2 Marks; Areas ( $0.0707 \text{ m}^2$  and  $0.0177 \text{ m}^2$ )- 1Mark

Computing Venturi head, from Bernoulli's Equation;  $h = 7.356 \text{ m}$  (3 Marks)

Discharge equation-2 Marks

$C_d = 0.979$  (2 Marks)

$h = x \left( \frac{S_m}{S} - 1 \right)$  (1 Mark)

$x = 0.472 \text{ m}$  (1 Mark)

- (b) Explanation with sketch..... **3 marks**

5. (a) 3 coefficients- 2 Marks each (**3\*2=6 Marks**)

- (b)  $L = 1 \text{ m}$ ,  $H = 0.3 \text{ m}$ ,  $n = 2$

Without considering velocity of approach,

$Q = \frac{2}{3} C_d \sqrt{2g} (L - 0.1nH) H^{1.5}$ .... 1 Mark

$= 0.2828 \text{ m}^3/\text{s}$ .....Substitution & answer 2 Marks

$A = 0.9 \times 2 = 1.8 \text{ m}^2$

$V_a = \frac{Q}{A} = 0.157 \text{ m/s}$ .... 1 mark

$h_a = \frac{V_a^2}{2g} = 0.00126 \text{ m}$ .... 1 mark

$H_1 = H + h_a$

Considering velocity of approach,

$Q = \frac{2}{3} C_d \sqrt{2g} (L - 0.1nH_1) (H_1^{1.5} - h_a^{1.5})$  .... 2 mark

= 0.2845 m<sup>3</sup>/s.....Substitution & answer 2 marks

**Total - 9 marks**

6. (a) Derivation of Euler's equation of motion..... 5 marks

Obtaining Bernoulli's equation..... 1 mark

Assumptions..... 2 marks

**Total - 8 marks**

- (b) Definition of orifice ..... 1 mark

Classification ..... 4 marks

**Total - 5 marks**

- (c) Cipolletti weir ....2 marks

**PART C**

7. (a) Derivation .....4 marks

Dupuit's equation  $\frac{L_e}{D_e^5} = \frac{L_1}{D_1^5} + \frac{L_2}{D_2^5} + \frac{L_3}{D_3^5}$  .....1 mark

**Total - 5 marks**

- (b)  $\mu = 0.097 \text{ Ns/m}^2$ ,  $\rho = 900 \text{ kg/m}^3$ , .....1 mark

$A = \frac{\pi}{4} \times 0.1^2 = 0.0079 \text{ m}^2$ ,  $Q = \frac{100}{900 \times 30} = 0.0037 \text{ m}^3/\text{s}$ .....2 marks

$V = \frac{Q}{A} = 0.471 \text{ m/s}$ .....1 mark

$Re = \frac{\rho VD}{\mu}$ .....1 mark

= 435 .....1 mark

Flow is laminar.....1 mark

$p_1 - p_2 = \frac{32\mu VL}{D^2}$  .....1 mark

= 1462 N/m<sup>2</sup> Substitution & answer 2 marks

**Total - 10 marks**

- (c) minor losses .....4 marks

major loss.....1 mark

**Total - 5 marks**

8. (a)  $\delta^* = \int_0^\delta (1 - \frac{v}{V}) dy$ ..... 2 marks

$\frac{v}{V} = \frac{y}{\delta}$

Substitution and simplification..... 1 mark

$\delta^* = \frac{\delta}{2}$ ..... 1 mark

$\theta = \int_0^\delta \frac{v}{V} (1 - \frac{v}{V}) dy$ ..... 2 marks

Substitution and simplification..... 2 marks

$\theta = \frac{\delta}{6}$ ..... 1 mark

$$\delta_E = \int_0^{\delta} \frac{v}{V} \left(1 - \left(\frac{v}{V}\right)^2\right) dy \dots\dots 2 \text{ marks}$$

Substitution and simplification..... 2 marks

$$\delta_E = \frac{\delta}{4} \dots\dots 1 \text{ mark}$$

**Total – 14 marks**

(b) Derivation of the Darcy-Weisbach equation with sketch - **6 marks**

9. (a)

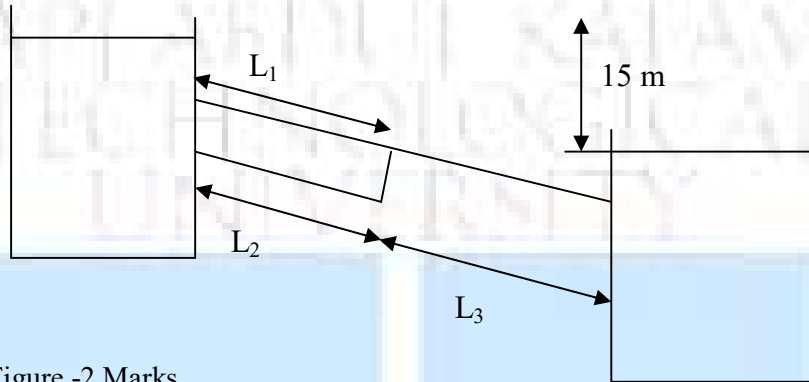


Figure -2 Marks

First case

$$15 = \frac{fLV^2}{2gD}$$

(2 Marks)

$$D = 0.256 \text{ m}$$

$$L = 1000 \text{ m}$$

$$hf_1 = hf_2$$

From which,

$$Q_1 = Q_2 \quad (2 \text{ Marks})$$

$$hf_1 + hf_3 = 15$$

$$Q_1 + Q_2 = Q_3 = 1.3Q_1 = 1.3 \times 0.1$$

$$\text{From which } Q_1 = Q_2 = 0.065 \text{ m}^3/\text{sec}$$

$$\frac{f_1 L_1 V_1^2}{2gD_1} + \frac{f_3 L_3 V_3^2}{2gD_3} = 15 \quad (2 \text{ Marks})$$

$$L_3 = L - L_1$$

$$V_1 = Q/A_1 \text{ and } V_3 = Q/A_3$$

$$\text{Substituting, } L_1 = 544.4 \text{ m} \quad (2 \text{ Marks})$$

(b) Figure ....2 marks

Explanation.....3 marks

**Total – 5 marks**

(c) Explanation with sketch..... **5 marks**