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## SAINTGITS COLLEGE OF ENGINEERING (AUTONOMOUS)

(AFFILIATED TO APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY, THIRUVANANTHAPURAM)

**FIFTH SEMESTER B.TECH DEGREE EXAMINATION (R,S), DECEMBER 2023**

**ROBOTICS AND AUTOMATION**

**(2020 SCHEME)**

**Course Code : 20RBT303**

**Course Name: Solid Mechanics**

**Max. Marks : 100**

**Duration: 3 Hours**

### PART A

*(Answer all questions. Each question carries 3 marks)*

1. Explain the significance of stress invariants.
2. Differentiate between plane stress and plane strain conditions.
3. State and explain generalized hooke's Law
4. Draw a true stress-strain curve for ductile material
5. State and explain the significance of section modulus
6. List the assumptions while deriving the torsional formula for a circular shaft.
7. State Maxwell's reciprocal relation
8. Write a short note on complementary strain energy.
9. What is slenderness ratio?
10. State Rankine's Theory for Maximum Normal Stress.

### PART B

*(Answer one full question from each module, each question carries 14 marks)*

#### MODULE I

11. a) At a point in a given material, the three-dimensional state of stress (12)  
is given by the following expressions.

$$\sigma_{xx}=\sigma_{yy}=\sigma_{zz}=10\text{N/mm}^2, \tau_{xy}=20\text{ N/mm}^2, \tau_{yz}=\tau_{xz}=10\text{N/mm}^2.$$

Find the stress invariants, principal stresses and principal plane.

- b) Explain the equality of cross shear (2)

#### OR

12. a) At a point in a bracket, the normal stress on two mutually (10)  
perpendicular planes are  $120\text{N/mm}^2$  tensile and  $60\text{N/mm}^2$  tensile.  
The shear stress across these planes is  $30\text{N/mm}^2$ . Find using  
Mohr's circle, the principle stresses and maximum shear stress.

- b) The displacement field is given by (4)

$$u=K(x^2+2z), v=K(4x+2y^2+z), w=4Kz^2 \text{ where } K \text{ is a constant.}$$

Find the component of stress at (2,2,3) directions.

## MODULE II

13. a) A steel bar is placed between two copper bars each having the same area and length as the steel bar at  $15^{\circ}\text{C}$ . At this stage, they are rigidly connected together at the ends. When the temperature is raised to  $315^{\circ}\text{C}$ , the length of the bars increases by  $1.50\text{mm}$ . Determine the original length and final stresses in the bars. Take  $E_s = 2.1 \times 10^5 \text{N/mm}^2$ ,  $E_c = 1 \times 10^5 \text{N/mm}^2$ ,  $\alpha_s = 0.000012 \text{ per}^{\circ}\text{C}$ ,  $\alpha_c = 0.0000175 \text{ per}^{\circ}\text{C}$  (12)
- b) What is Poisson's Ratio? (2)

## OR

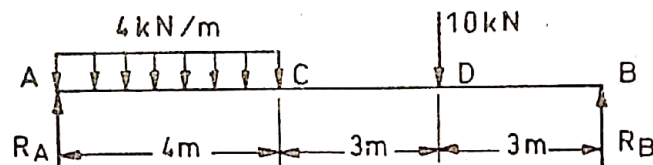
14. a) Write the stress-strain relationship for linear elastic isotropic materials in terms of Young's modulus and Poisson's ratio (5)
- b) A bar of  $40 \text{ mm}$  diameter is subjected to a pull of  $50\text{kN}$ . The measures extension on gauge length of  $200\text{mm}$  is  $0.1\text{mm}$  and the change in diameter is  $0.004\text{mm}$ . Calculate (9)
- Young's Modulus
  - Poisson's Ratio
  - Bulk Modulus

## MODULE III

15. a) A solid shaft  $125\text{mm}$  in diameter transmits  $120\text{kW}$  at  $160 \text{ rpm}$ . Find the maximum shear stress induced in the shaft. Find also the angle of twist in the length of  $7.5 \text{ m}$ . Take  $G = 8 \times 10^4 \text{N/mm}^2$  (7)
- b) A solid shaft of  $200 \text{ mm}$  diameter has the same cross-sectional area as that of a hollow shaft of the same material with an inside diameter of  $150\text{mm}$ . Find the ratio of power transmitted by the two shafts at the same speed. (7)

## OR

16. a) Draw shear force and bending moment diagrams for the beam shown in figure and find the maximum bending moment and the location. (7)



- b) Compare the strength of a hollow shaft of diameter ratio  $0.75$  to that of a solid shaft by considering the permissible shear stress. Both the shafts are of same material, of same length and weight. (7)

**MODULE IV**

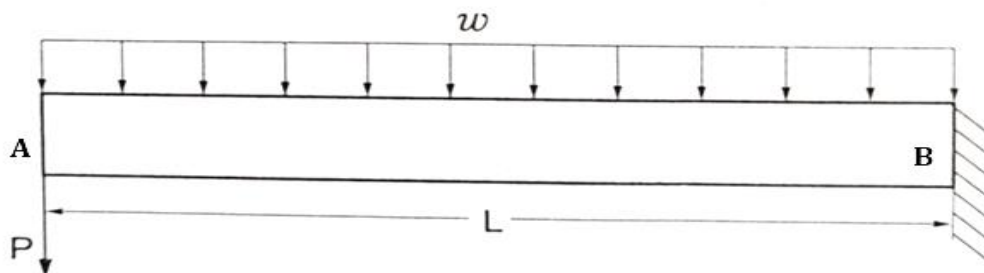
17. A beam of length 6m is simply supported at its ends and carries two point loads of 48 kN and 40 kN at a distance of 1m and 3m respectively from the left support. Find the following: (14)

- (i) deflection under each load.
- (ii) maximum deflection
- (iii) the point at which maximum deflection occurs.

Take  $E = 2 \times 10^5 \text{ N/mm}^2$  and  $I = 85 \times 10^6 \text{ mm}^4$

**OR**

18. a) A cantilever beam AB supports a uniformly distributed load  $w$  and a concentrated load  $P$  as shown in fig. It is given that  $L = 2\text{m}$ ,  $w = 4\text{kN/m}$ ,  $P = 6\text{kN}$  and  $EI = 5\text{MN.m}^2$ . Determine deflection at point A. (7)



- b) Derive an expression for strain energy due to (i) bending load and (ii) Axial loading (7)

**MODULE V**

19. a) A hollow alloy tube 5m long is having external and internal diameters equal to 40mm and 25mm respectively under a tensile load. Find the Euler's buckling load for the tube, when used as a column with both ends fixed. Also, find the safe compressive load for the tube with a factor of safety 4. (7)

Assume  $E = 2 \times 10^5 \text{ N/mm}^2$  and  $I = 15 \times 10^9 \text{ mm}^4$

- b) A hollow cylindrical cast iron is 4 meters long, both ends being fixed. Design the column to carry an axial load of 250kN. Use Rankine's formula and adopt a factor of safety of 5. The internal diameter may be taken as 0.80 times the external diameter. Take  $\sigma_c = 550\text{N/mm}^2$  and  $\alpha = 1/1600$  (7)

**OR**

20. a) Derive the equation to find a crippling load of columns when both ends are hinged by using Euler's theory. (5)
- b) The stress induced at a critical point in a machine component ( $\sigma_{\text{yield}} = 360 \text{ N/mm}^2$ ) are  $\sigma_{xx} = 150 \text{ N/mm}^2$ ,  $\sigma_{yy} = 60 \text{ N/mm}^2$ ,  $\tau_{xy} = 45 \text{ N/mm}^2$ . Calculate the factor of safety based on (i) Maximum shear stress theory, (ii) Maximum normal stress theory (iii) Distortion energy theory. (9)

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