

Register No.: Name:

SAINTGITS COLLEGE OF ENGINEERING (AUTONOMOUS)

(AFFILIATED TO APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY, THIRUVANANTHAPURAM)

**FIFTH SEMESTER INTEGRATED MCA DEGREE EXAMINATION (R), DECEMBER 2023
(2020 SCHEME)****Course Code: 20IMCAT301****Course Name: Numerical Methods****Max. Marks: 60****Duration: 3 Hours*****Non-programmable calculator may be permitted in the examination hall.*****PART A*****(Answer all questions. Each question carries 3 marks)***

1. Find AB and BA for the matrices $A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix}$ and $B = \begin{bmatrix} -7 & -8 \\ 9 & 10 \\ 0 & -11 \end{bmatrix}$.
2. Find the inverse of the given matrix, if it exists, $A = \begin{bmatrix} 1 & 1 \\ 3 & 4 \end{bmatrix}$.
3. Determine whether the following system of equations is consistent:

$$\begin{aligned} x + y - z &= 1 \\ x + y - z &= 0 \end{aligned}$$
4. Find the rank of the given matrices:
 - (i) $A = \begin{bmatrix} 1 & 2 & 0 \\ 3 & 1 & -5 \end{bmatrix}$
 - (ii) $B = \begin{bmatrix} 4 & 1 \\ 2 & 3 \\ 2 & 2 \end{bmatrix}$
5. The product of two eigen values of the matrix $A = \begin{bmatrix} 6 & -2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{bmatrix}$ is 16.
Find the third eigen value of A.
6. Find the sum and product of the eigen values of the matrix $A = \begin{bmatrix} 3 & 1 & -1 \\ 0 & 2 & 6 \\ 0 & 0 & 6 \end{bmatrix}$.
7. Define principle of least squares.
8. What are the normal equations for fitting of a straight line $y = ax + b$.
9. Explain Lagrange's interpolation formula.
10. Estimate the value of $f(7)$ from the following data using Newton's divided difference interpolation formula:

| | | | | |
|---|----|----|----|----|
| x | 5 | 6 | 9 | 11 |
| y | 12 | 13 | 14 | 16 |

PART B

(Answer one full question from each module, each question carries 6 marks)

MODULE I

11. a) Define trace of a matrix. Find the trace of the matrix

$$A = \begin{bmatrix} 3 & 0 & 1 \\ 1 & 0 & 2 \\ 0 & 0 & 1 \end{bmatrix}. \quad (2)$$

- b) Find the inverse of the matrix $A = \begin{bmatrix} 0 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 3 \end{bmatrix}$ using Gauss-Jordan method. (4)

OR

12. a) Define symmetric and skew-symmetric matrices with examples. (3)

- b) Show that $AB = CB$ but $A \neq C$ for $A = \begin{bmatrix} 3 & 2 \\ 1 & 0 \end{bmatrix}$, $B = \begin{bmatrix} 2 & 4 \\ 1 & 2 \end{bmatrix}$,
 $C = \begin{bmatrix} 1 & 6 \\ 3 & -4 \end{bmatrix}$. (3)

MODULE II

13. Write the set of equations associated with the given augmented matrix and the specified variables and then solve. (6)

$$[A|B] = \begin{bmatrix} 0 & 0 & 2 & 3 & 0 \\ 1 & 0 & 3 & 1 & 0 \\ 1 & 1 & 2 & 0 & 0 \end{bmatrix}, x_1, x_2, x_3, x_4.$$

OR

14. Use Gaussian elimination method to solve the system of equations:

$$\begin{aligned} x + 3y + 2z &= 0 \\ -x - 4y + 3z &= -1 \\ 2x - z &= 3 \\ 2x - y + 4z &= 2 \end{aligned} \quad (6)$$

MODULE III

15. Find the eigen values and eigen vectors of the matrix (6)

$$A = \begin{bmatrix} 2 & 1 & -1 \\ 1 & 1 & -2 \\ -1 & -2 & 1 \end{bmatrix}.$$

OR

16. Diagonalize the matrix $A = \begin{bmatrix} 1 & 0 & -1 \\ 1 & 2 & 1 \\ 2 & 2 & 3 \end{bmatrix}$. (6)

MODULE IV

17. Apply method least squares to fit an equation of the form $y = a + bx$ to the following data:

| | | | | | |
|---|----|----|----|----|----|
| x | 1 | 2 | 3 | 4 | 5 |
| y | 12 | 25 | 38 | 47 | 65 |

(6)

OR

18. Analyze the following data to fit a second-degree parabola of the form $y = a + bx + cx^2$.

| | | | | | |
|---|-----|-----|-----|-----|-----|
| x | 0 | 1 | 2 | 3 | 4 |
| y | 1.2 | 1.7 | 2.1 | 2.8 | 5.9 |

(6)

MODULE V

19. Compute the approximate value of $f(0.25)$ using Newton's forward interpolation formula from the following data:

| | | | | | |
|---|---|--------|--------|--------|--------|
| x | 0 | 0.5 | 1 | 1.5 | 2 |
| y | 1 | 1.0513 | 1.1052 | 1.1618 | 1.2214 |

(6)

OR

20. Use Lagrange's interpolation formula to find the value of y , when $x = 10$ from the following data:

| | | | | |
|---|----|----|----|----|
| x | 5 | 6 | 9 | 11 |
| y | 12 | 13 | 14 | 16 |

(6)
