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Reg. No. _____ Name: _____

**APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY
SECOND SEMESTER B.TECH DEGREE SPECIAL EXAMINATION, AUGUST 2016****Course Code: MA-102****Course Name: DIFFERENTIAL EQUATIONS**

Max. Marks: 100

Duration: 3 hrs

PART A*Answer all questions Each carries 3 marks*

1. Find ordinary differential equation for the basis $e^{-x\sqrt{2}}$, $xe^{-x\sqrt{2}}$
2. Reduce $y'' = y'$ to 1st order differential equation and solve.
3. Find the particular solution to $(D^4 - m^4) y = \sin mx$
4. Use variation of parameters to solve $y'' + y = \sec x$
5. Find the Fourier coefficient a_n for the function $f(x) = 1 + |x|$ defined in $-3 < x < 3$
6. Develop the Fourier Sine series of $f(x) = x$ in $0 < x < \pi$
7. Obtain the partial differential equation by eliminating arbitrary function from $x^2 + y^2 + z^2 = f(xy)$
8. Solve $y^2 zp + x^2 zq = xy^2$
9. Solve $u_x + u_y = 0$ using method of separation of variables
10. A finite string of length L is fixed at both ends and is released from rest with a displacement $f(x)$. What are the initial and boundary conditions involved in this problem?
11. Write all the possible solutions of one-dimensional heat transfer equation
12. Find the steady state temperature distribution in a rod of length 30cm having the ends at 20°C and 80°C respectively.

PART B*Answer one full question from each module***Module -I**

13. (a) Verify linear independence of $e^{-x}\cos x$ and $e^{-x}\sin x$ using Wronskian and hence solve the initial value problem $y'' + 2y' + 2y = 0$, $y(0) = 0$, $y'(0) =$
15

(b) Find the general solution of the equation $x^2y'' + xy' + (x^2 - 0.25)y = 0$

If $y_1 = \frac{\cos x}{\sqrt{x}}$

OR

14. (a) Find a second order homogeneous linear ODE for which x , $x \log x$ are solutions and solve the IVP with $y(1) = 2$, $y'(1) = 4$.

(b) Solve the IVP $y'' - 4y' + 9y = 0$, $y(0) = 0$, $y'(0) = -8$

Module- II

15. (a) Solve $(D^2 - 2D + 5)y = e^{2x} \sin x$

(b) Solve $((x + 1)^2 \frac{d^2y}{dx^2} + (x + 1) \frac{dy}{dx} = (2x + 3)(2x + 4)$

OR

16. (a) Solve $x^3 \frac{d^3y}{dx^3} + 2x^2 \frac{d^2y}{dx^2} + 2y = 10 \left(x + \frac{1}{x}\right)$

(b) Solve $y'' - 4y' + 5y = \frac{e^{2x}}{\sin x}$ by method of variation of parameters

Module - III

17. (a) Find the Fourier series representation of $f(x) = x \sin x$ periodic with period 2π , defined in $0 < x < 2\pi$

(b) Find the Fourier cosine series of $f(x) = \cos x$, $0 < x < \pi/2$

OR

18. (a) Find the Fourier series expansion of $f(x) = e^{-x}$ in $-c < x < c$

(b) Develop the Sine series representation of $f(x) = \begin{cases} x, & 0 < x < 2 \\ 4 - x, & 2 < x < 4 \end{cases}$

Module - IV

19. (a) Solve $(y + zx)p - (x + yz)q = x^2 - y^2$

(b) Find the differential equation of all spheres of fixed radius having their centres in XY -plane.

OR

20. (a) Solve $(D^2 - 2DD' - 15D'^2)z = 12xy$

(b) Find the particular integral of

$$(D^3 - 7DD'^2 - 6D'^3)z = \sin(x + 2y) + e^{3x+y}$$

Module – V

21. A tightly stretched homogeneous string of length 20cm with its fixed ends executes transverse vibrations. Motion starts with zero initial velocity by displacing the string into the form $f(x) = K(x^2 - x^3)$. Find the deflection $u(x, t)$ at any time t .

OR

22. A tightly stretched string of length 'a' with fixed ends is initially in equilibrium position. Find the displacement $u(x, t)$ of the string if it is set vibrating by giving each of its points a velocity $v_0 \sin^3\left(\frac{\pi x}{a}\right)$.

Module - VI

23. Find the temperature distribution in a rod of length 2m whose end points are maintained at temperature zero and the initial temperature $f(x) = 100(2x - x^2)$

OR

24. The temperatures at the ends of a bar of length l cm with insulated sides are $30^\circ C$ and $90^\circ C$ respectively until steady state conditions prevail. If the temperature at each end is then suddenly reduced to $0^\circ C$ and maintained so, find the temperature distribution at a distance x at time t .