# SAINTGITS COLLEGE OF ENGINEERING (AUTONOMOUS) 

(AFFILIATED TO APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY, THIRUVANANTHAPURAM) FOURTH SEMESTER INTEGRATED MCA DEGREE EXAMINATION (R), MAY 2023 (2020 SCHEME)
Course Code: 20IMCAT204

Course Name: Statistical Applications
Max. Marks: 60
Duration: 3 Hours
Statistical tables and non-programmable Scientific calculators up to Casio Fx991 ESPlus may be permitted in the examination hall

PART A
(Answer all questions. Each question carries 3 marks)

1. Distinguish between positive and negative correlation.
2. The coefficient of correlation between two variables $X$ and $Y$ is 0.48 . The covariance is 36 . The variance of X is 16 . Find the standard deviation of Y .
3. For two variables x and y with the same mean, the regression equations are $y=x+a$ and $\quad x=3 y+b$. Then find $\frac{a}{b}$.
4. If the regression equations of y on x and x on y are: $y=\frac{4}{5}+0.3 x$ and $x=\frac{1}{6}+$ $0.5 y$, find the coefficient of correlation between x and y .
5. Define (i) Parameter and (ii) Statistic.
6. Suppose that X is a random variable with mean $\mu$ and variance $\sigma^{2}$. Let $X_{1}, X_{2}, \ldots, X_{n}$ be a random sample of size $n$ from the population represented by X. Show that sample mean $\bar{X}$ is an unbiased estimator of the population mean $\mu$.
7. Define (i) Null hypothesis and (ii) Alternative hypothesis.
8. In order to test whether a coin is perfect, it is tossed 5 times. The null hypothesis of perfectness is rejected if and only if more than 4 heads are obtained. Find the probability of type I error.
9. Write down the three assumptions for Student's $t$ test.
10. What are the conditions for the validity of chi-square test?

PART B
(Answer one full question from each module, each question carries 6 marks)

## MODULE I

11. Calculate the Karl Pearson's coefficient of correlation between expenditure on advertising and sales from the data given below

| Advertising expenses (‘000 Rs) | 40 | 66 | 63 | 91 | 83 | 76 | 26 | 99 | 37 | 79 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Sales (Lakh Rs) | 46 | 52 | 57 | 85 | 61 | 67 | 59 | 90 | 50 | 83 |

## OR

12. Two judges in a beauty competition rank the 12 entries as follows:

| X | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Y | 12 | 9 | 6 | 10 | 3 | 5 | 4 | 7 | 8 | 2 | 11 | 1 |

What degree of agreement is there between the two judges.

## MODULE II

13. For 50 students of a class, the regression equation of marks in Statistics (y) on the marks in Accountancy (x) is $4 y-5 x-8=0$. Average marks in Accountancy are 40. The ratio of the standard deviations $\sigma_{y}: \sigma_{x}$ is 5:2. Find the average marks in Statistics and the coefficient of correlation between the marks in two subjects.

## OR

14. From the following data, obtain the two regression equations:

| x | 90 | 96 | 107 | 120 | 66 | 123 | 50 | 72 | 110 | 56 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| y | 72 | 76 | 70 | 98 | 71 | 92 | 40 | 62 | 81 | 48 |

## MODULE III

15. Distinguish between simple random sampling and stratified random sampling.

## OR

16. Find the maximum likelihood estimate for variance of normal distribution.

## MODULE IV

17. It is claimed that a random sample of 100 tyres with a mean life of 15269 kms is drawn from a population of tyres which has a mean life of 15200 kms and a standard deviation of 1248 kms . Test the validity of the claim at $5 \%$ level of significance.

## OR

18. A machine puts out 16 imperfect articles in a sample of 500 . After the machine is overhauled, it puts out 3 imperfect articles in a batch of 100. Has the machine improved?

## MODULE V

19. Ten cartons are taken at random from an automatic filling machine. The mean net weight of the 10 cartons is 11.8 oz . and standard deviation is 0.15 oz . Does the sample mean differ significantly from the intended weight of 12 oz at $5 \%$ level of significance?
20. It is known that the mean diameters of rivets produced by two firms A and $B$ are practically the same but the standard deviations may differ. For 22 rivets produced by firm A, the standard deviation is 2.9 mm while for 16 rivets manufactured by firm $B$, the standard deviation is 3.8 mm . Test whether the products of firm A have the same variability as those of firm B at 5\% level of significance.
