## SAINTGITS COLLEGE OF ENGINEERING (AUTONOMOUS)

(AFFILIATED TO APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY, THIRUVANANTHAPURAM)

## FIFTH SEMESTER B.TECH DEGREE EXAMINATION (S), FEBRUARY 2023 COMPUTER SCIENCE AND ENGINEERING

 (2020 SCHEME)
## Course Code : 20CST301

Course Name: Formal Languages and Automata Theory
Max. Marks : 100
Duration: 3 Hours

## PART A

(Answer all questions. Each question carries 3 marks)

1. Define Non Deterministic Finite Automata? Compare its ability with Deterministic Finite Automata in accepting languages.
2. Design a Finite state automata which accepts all binary strings over $\{0,1\}$ that are divisible by 3.
3. Construct regular expression for the language that consists of all strings ending with 00 . Assume $\Sigma=\{0,1\}$
4. Define Ultimate Periodicity.
5. State Myhill-Nerode Theorem and its applications.
6. When do you say a CFG is ambiguous?
7. List any three Closure properties of Context Free Language.
8. Explain 2 types of language acceptance by PDA.
9. Write the formal definition of Context Sensitive Grammar. Write the CSG for the language $L=\left\{a^{n} b^{n} c^{n} \mid n>=1\right\}$.
10. Write a note on Recursive Enumerable Languages.

PART B
(Answer one full question from each module, each question carries 14 marks)

## MODULE I

11. a) Prove the equivalence of non deterministic finite automata and deterministic finite automata.
b) Convert the following NFA to DFA


OR
12. a) Design a Finite state automata which accepts all strings over $\{0,1\}$ with Odd number of 0's or even number of 1's. Show the changes needed to convert the above designed automata to accept, odd number of 0's and even number of 1 's.
b) What is $\varepsilon$-closure? Find the $\varepsilon$-closure of the following NFA.


MODULE II
13. a) Prove that $\mathrm{L}=\left(\mathrm{a}^{\mathrm{p}} \mid \mathrm{p}\right.$ is a prime number $\}$ is not regular.
b) Minimize the following DFA using equivalence theorem.


## OR

14. a) Design an $\varepsilon$-NFA for the regular expression $(0+1) * 01$.
b) State Arden's Theorem .Convert the following finite automata to regular expression.


## MODULE III

15. a) Minimize the following DFA by table filling method using MyhillNerode theorem describing the steps in detail.

b) Write regular expression corresponding to following languages
i) $\quad \mathrm{L}=\left\{\mathrm{a}^{\mathrm{n}} \mathrm{b}^{\mathrm{m}} \mid \mathrm{n}>=4, \mathrm{~m}<=3\right\}$
ii) $L=\left\{\mathrm{w} \in \sum^{*} \mid\right.$ Every string in $L$ begins with 00 and ends with 11 over $\left.\sum=(0,1)\right\}$

## OR

16. a) Convert the following CFG to Greibach Normal Form
$S \rightarrow X A \mid B B$
$\mathrm{B} \rightarrow \mathrm{b} \mid \mathrm{SB}$
$\mathrm{X} \rightarrow \mathrm{b}$
$\mathrm{A} \rightarrow \mathrm{a}$
b) Convert the following CFG into CNF
$S \rightarrow$ ASA $\mid a B$
$\mathrm{A} \rightarrow \mathrm{B} \mid \mathrm{S}$
$B \rightarrow b \mid \varepsilon$

## MODULE IV

17. a) Construct a Deterministic PDA for the language $L=w w^{R}$ over $\sum=\{a, b\}$. Is this a Deterministic PDA. Justify your answer. Otherwise how can we modify this language to make it accepted by DPDA.
b) State pumping lemma for CFL. Write its application.

## OR

18. a) Compare context sensitive grammar and context free grammar. Can we design a PDA for context sensitive languages? Justify your answer.
b) Convert the following PDA to equivalent CFG
$\partial\left(q_{0}, a, Z_{0}\right)=\left(q_{0}, Z_{0}\right)$
$\partial\left(q_{0}, \mathrm{~b}, \mathrm{Z}_{0}\right)=\left(\mathrm{q}_{0}, \mathrm{~b} Z_{0}\right)$
$\partial\left(q_{0}, a, a\right)=(q o, a a)$
$\partial\left(\mathrm{q}_{\mathrm{o}}, \mathrm{b}, \mathrm{b}\right)=(\mathrm{q}, \mathrm{bb})$
$\partial\left(\mathrm{q}_{0}, \mathrm{a}, \mathrm{b}\right)=\left(\mathrm{q}_{0}, \varepsilon\right)$
$\partial\left(\mathrm{q}_{0}, \mathrm{~b}, \mathrm{a}\right)=\left(\mathrm{q}_{0}, \varepsilon\right)$

## MODULE V

19. a)

Design a Turing Machine over $\sum=\{0,1,2\}$ to accept $L=\left\{0^{n} 1^{n} 2^{\mathrm{n}} \mid \mathrm{n}>1\right\}$
b) Explain different type of Turing Machine.

## OR

20. a) Prove that halting problem of Turing machine is undecidable.
b) Explain Chomsky's Hierarchy of Languages.
