# APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY FIRST SEMESTER M. TECH DEGREE EXAMINATION Civil Engineering (Structural Engineering and Construction Management) 04CE6403—THEORY OF ELASTICITY

Max. Marks: 60

**Duration: 3 Hours** 

# PART A

# Answer All Questions

### Each question carries 3 marks

- 1. Briefly explain surface forces and body forces.
- 2. Write the stress strain relations for plane strain problems.
- 3. Explain St. Venant's principle and its applications.
- 4. Discuss the effect of geometrical irregularities on the distribution of stresses.
- 5. List the assumptions involved in Coloumb's theory for torsion of circular shafts.
- 6. Discuss Prandtl's stress function approach for the solution of twisted bars.
- 7. Explain Stress- strain curve for mild- steel up to rupture.
- 8. Write short note on plastic potential.

# PART B

#### Each question carries 6 marks

9. The state of stress at a point in a material is given by  $\sigma_x = \sigma_y = \sigma_z = 10 \text{ N/mm}^2$ .  $\tau_{xy} = 20 \text{ N/mm}^2$ ,  $\tau_{xz} = \tau_{yz} = 10 \text{ N/mm}^2$ . Find the principal stresses and the direction of major principal stress.

#### OR

- 10. Derive the equations of equilibrium in Cartesian coordinate system.
- 11. Show that the stress distribution is same for all isotropic materials in two dimensional state of stress.

OR

- 12. Derive the compatibility equation in terms of stresses. Explain its significance.
- 13. Briefly explain Airy's stress function approach in solving boundary value problems in elasticity.

OR

- 14. Using the stress function,  $\oint = -\left(\frac{3F}{h^2}\right)xy^2 + \left(\frac{2F}{h^3}\right)xy^3$ , find and plot the variations of stress components in a region included in *y*=0, *y*=*h*, *x*=0 and *x*=*L*.
- 15. Derive expressions for the radial and tangentive stresses in a thick cylinder subjected to internal and external stresses.

- 16. Derive expression for the stresses in a rotating disc of uniform thickness and mass density.
- 17. Briefly explain Prandtl's membrane analogy.

#### OR

18. A hollow aluminium tube of rectangular cross section is subjected to a torque of 56,500 Nm along its longitudinal axis. Determine the shearing stresses and angle of twist. Take  $G= 27.6 \ x10^9 \ N/m^2$ . (All thickness in metres)



19. Define,

- a) Rigid material
- b) Perfectly linear elastic material
- c) Rigid perfectly plastic material

OR

20. Explain yield criteria. Explain Tresca's yield criterion and Von Mises yield criterion.