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# APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY FIFTH SEMESTER B.TECH DEGREE EXAMINATION, DECEMBER 2017 <br> <br> Course Code: AE307 <br> <br> Course Code: AE307 <br> Course Name: SIGNALS AND SYSTEMS (AE) 

Max. Marks: 100
Duration: 3 Hours

## PART A

Answer any two full questions, each carries 15 marks.
1 a) Differentiate between energy and power signals with suitable examples.
b) Determine the response of the following system with impulse response and input signal as follows: $h[n]=\left(\frac{1}{2}\right)^{n} u[n]$ and $x[n]=2^{n} u[n]$
c) Check whether the following systems is static/dynamic, linear /nonlinear, timeinvariant or variant and causal /non-causal. $y(t)=A x(t)+B$
2 a) Evaluate the step response of the system represented by the impulse response.

$$
\begin{equation*}
h[n]=\left(\frac{1}{2}\right)^{n} u[n] . \tag{5}
\end{equation*}
$$

b) Find the odd and even components of the signal $x(t)=e^{-2 t}$ cost.
c) Find the convolution of the following sequence.

$$
\begin{gather*}
x[n]=2 \delta[n+1]-\delta[n]+\delta[n-1]+3 \delta[n-2]  \tag{5}\\
h[n]=3 \delta[n-1]+4 \delta[n-2]+2 \delta[n-3]
\end{gather*}
$$

3 a) Determine the stability of the system described by difference equation.

$$
\begin{equation*}
y[n]-\frac{5}{2} y[n-1]+y[n-2]=x[n]-x[n-1] \tag{10}
\end{equation*}
$$

b) State and prove Distributive property of convolution.

## PART B

Answer any two full questions, each carries 15 marks.
4 a) Find the trigonometric Fourier series for the continuous time periodic signal

$$
\begin{array}{r}
x(t)=1 \text { for } 0 \leq t<1 \\
=-1 \text { for } 1 \leq t<2 \tag{7}
\end{array}
$$

b) Find the Fourier transform of $x(t)=5 \sin ^{2}(3 t)$

5 a) Find the Fourier transform of the signal $x[n]=\{2,1,-1,-2\}$
b) Find the convolution of the signals given below using Fourier transform

$$
\begin{equation*}
x_{1}[n]=\left(\frac{1}{2}\right)^{n} u[n] ; \quad x_{2}[n]=\left(\frac{1}{3}\right)^{n} u[n] \tag{5}
\end{equation*}
$$

6 a) Explain the condition for distortion less transmission through an LTI system
b) What is Hilbert transform? Explain the properties of Hilbert transform.

## PART C

## Answer any two full questions, each carries 20 marks.

7 a) State and prove convolution property of Laplace Transform.
b) Find the impulse and step response of the following system

$$
\begin{equation*}
H(s)=\frac{s+2}{s^{2}+5 s+4} \tag{10}
\end{equation*}
$$

8 a) Find the z-transform and ROC for the signal $x[n]=2^{n} u[n]$.
b) Plot the pole-zero pattern and determine whether the following system are stable or not $y[n]=y[n-1]-0.5 y[n-2]+x[n]+x[n-1]$
9 a) Find the output of the system using z-transform whose input and out related by $y[n]=7 y[n-1]-12 y[n-2]+2 x[n]-x[n-2]$ for input $x[n]=u[n]$
b) For the transfer function $H(s)=\frac{s+10}{s^{2}+3 s+2}$ find the response due to the input $x(t)=\sin (2 t) u(t)$.

