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APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY FIFTH SEMESTER B.TECH DEGREE EXAMINATION(S), MAY 2019

Course Code: AE301

Course Name: CONTROL SYSTEM

Max. Marks: 100

Duration: 3 Hours

Marks

(3)

(Use appropriate graph sheets if required)

PART A

Answer any two full questions, each carries 15 marks.

- 1 a) Compare open loop and closed loop systems.
 - b) Obtain the differential equations governing the mechanical system shown below and draw the *force-voltage* electrical analogous circuit



c) A unity feedback system has the following forward path transfer function. (4) $G(s) = \frac{180}{s(s+6)} \text{and} r(t) = 4t.$ Determine the corresponding static error

coefficient and the steady state error.

- 2 a) Compare any two features of transient and steady state part of the system (2) response.
 - b) Obtain overall transfer function for the given system using Mason's gain formula (10)



c) Define type and order of a system. Give one example.

(3)

E1101

(6)

3 Find the transfer function of the given system using block diagram reduction (7) a) method. Draw the corresponding signal flow graph also.



b) A unity feedback system has the following open loop transfer function, where **K** (8) and T are constants. Determine the factor by which K should be multiplied to reduce the overshoot from 85% to 35%.

$$G(s) = \frac{K}{s(1+sT)}$$

PART B

Answer any two full questions, each carries 15 marks.

- 4 Explain the effect of addition of zeros to the root locus and system stability. a) (3)
 - Given the characteristic equation of a system. Using R.H criterion, Find the (6) b) location of roots in s-plane and hence comment whether the system is fully stable, unstable or conditionally stable.

$$F(s) = s^4 + 2s^3 + 11s^2 + 18s + 18 = 0$$

sketch the polar plot for the open loop transfer function c)

$$G(s) = \frac{8}{(s+1)(s+2)}$$

- 5 Define the terms phase margin and gain margin. What is the value of gain (3) a) margin in dB for critically stable system?
 - b) Sketch the root locus for the given open loop transfer function and find the value of *K* and ω for marginal stability where *K*>0. (*use graph sheet*).

$$G(s)H(s) = \frac{K}{s(s+2)(s+3)}$$
(12)

a) Differentiate minimum and non-minimum phase system. Give example. 6 (3)

А

b) A unity feedback control system with given G(s), draw the Bode plot. Find the gain margin and phase margin. Also check for the stability. (*Use semi-log sheet*) (12)

$$G(s) = \frac{5(1+2s)}{(1+4s)(1+0.25s)}$$

PART C

Answer any two full questions, each carries20 marks.

- 7 a) Define the terms state variable and state space. Mention any four distinct (6) advantages of state space representation.
 - b) Obtain the state model for the electrical network shown.

(6)



c) Determine the transfer function of a system represented by

$$\dot{X} = \begin{bmatrix} -2 & -2 \\ 4 & -8 \end{bmatrix} X + \begin{bmatrix} 1 \\ 1 \end{bmatrix} U; \quad Y = \begin{bmatrix} 1 & 0 \end{bmatrix} U$$
(8)

- 8 a) Mention any four properties of state transition matrix. (4)
 - b) An LTI system is represented by the state equation $\dot{X} = A X + BU$, where
 - $A = \begin{bmatrix} 0 & 1 & 2 \\ 0 & 3 & 4 \\ 1 & 3 & 2 \end{bmatrix} \text{ and } B = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}, \text{ find the characteristic equation and the poles of the }$ (8)

system. Comment on the system stability.

c) Mention the advantage of diagonalization of system matrix in state space (8) analysis. Discuss the methods for diagonalization. Find the eigen values of matrix $A = \begin{bmatrix} 3 & -2 \\ -1 & 2 \end{bmatrix}$ and also diagonalize the given matrix without calculating eigenvectors.

- 9 a) Define controllability and observability of a system. (2)
 - b) Express the following transfer function in controllable canonical form. Draw the corresponding signal flow graph also.

$$\frac{Y(s)}{U(s)} = \frac{5s^2 + 2s + 6}{s^3 + 7s^2 + 11s + 8}$$
(10)

c) Check the controllability and observability of the following system.

$$\dot{X} = \begin{bmatrix} -1 & 0\\ 0 & -2 \end{bmatrix} X + \begin{bmatrix} 0\\ 1 \end{bmatrix} U; \quad Y = \begin{bmatrix} 1 & 2 \end{bmatrix} X$$
(8)
