Reg No.: Name:										_				
		A	PJ ABDUL				GICA	L UNI	VERSI	TY				
	F(OURTH SE	MESTER B					TION(S), DE	CEMBER 201	19			
(Cour	rse Name: P	ROBABILI		TRIBU	ode: MA TIONS, THODS		SFOR	MS A	ND NUMERIO	CAL			
M	ax. I	Marks: 100								Duration: 3	Hours			
		Ι	Normal distri	PART A	A (MOI		I AND		ition h	all.				
1	a)	The following table gives the probability that a certain computer will malfunction												
		0, 1, 2, 3, 4, 5, or 6 times on any one day												
		Number of	. X	0	1	2	3	4	5	6				
		Malfunctio	ons											
		Probability	f(x)	0.17	0.29	0.27	0.16	0.07	0.03	0.01	(7)			
		Find (i) Th	e Mean, Vari	ance and	d Standa	ard Devi	ation of	this p	obabili	ty distribution				
	(ii) $P(0 < x < 5)$ (iii) $P(x > 4)$													
	b)	It is know	n that 5%	of the b	ooks b	ound at	a cert	ain bii	ndery 1	have defective				
		bindings. Find the probability that atmost 2 of 100 book bound by this bindery												
have defective binding using									(8)					
		(i)	The formula	for bino	mial dis	stributio	n				(0)			
		(ii)	Poisson appr	oximati	on to the	e binomi	al distri	bution						
2	a) Derive the mean, variance and distribution function of the uniform distribut										(7)			
	the interval (a,b).													
	b)	The amour	nt of time that	t a surve	illance c	amera v	vill run	withou	t havin	g to be reset is				
		a random variable having the exponential distribution with mean 50 days.												
		Find the pr	obability tha	t such a	a camera will									
		(i)	have to be re	eset in le	ss than 2	20 days					(8)			
		(ii)	not have to b	e reset i	n at leas	st 60 day	'S							
		(iii)	have to be re	set betw	een 20	and 60 d	ays.							
3	a)	The time required to microwave a bag of popcorn using the automatic setting can												
		be treated	as a rando	m varia	ible hav	ving a	normal	distrib	oution	with standard				
	deviation 10 seconds. If the probability is 0.8212 that the ba									g will take less than (7				
		282.5 seconds to pop, find the probability that it will take longer than 258.3												

seconds to pop.

b) Prove that binomial distribution with parameters n and p can be approximated to Poisson distribution when n is large and p is small with $np = \lambda$, a constant.

PART B (MODULES III AND IV)

Answer two full questions.

- Use Fourier integral to show that $\int_0^\infty \frac{\cos x\omega + \omega \sin x\omega}{1 + \omega^2} d\omega = \begin{cases} 0 & \text{if } x < 0 \\ \pi/2 & \text{if } x = 0 \\ \pi e^{-x} & \text{if } x > 0 \end{cases}$ (7)
 - b) Find the Fourier Sine and Cosine Transform of $f(x) = \begin{cases} x^2 & \text{if } 0 < x < 1 \\ 0 & \text{if } x > 1 \end{cases}$ (8)
- 5 a) Find the Laplace Transform of:
 - (i) $e^{-t} \sin 3t \cos 2t$
 - (ii) $t^2 \cos \omega t$ (7)
 - (iii) $t^2u(t-1)$
 - b) Find the inverse Laplace Transform of:
 - (i) $\frac{1-7s}{(s-3)(s-1)(s+2)}$
 - (ii) $\ln \frac{s-a}{s-b}$ (8)
 - (iii) $\frac{e^{-3s}}{(s-1)^3}$
- 6 a) Find the Fourier Sine Transform of $f(x) = e^{-|x|}$. Hence evaluate $\int_0^\infty \frac{\omega \sin x \omega}{1 + \omega^2} d\omega$. (7)
 - b) Solve by using Laplace Transform: $y'' + 2y' 3y = 6e^{-2t}$, y(0) = 2, y'(0) = -14 (8)

PART C (MODULES V AND VI)

Answer two full questions.

- 7 a) Find the positive solution of $2\sin x = x$ using Newton Raphson (method correct to five decimal places). (6)
 - b) Find the value of tan 33⁰ by using Lagrange's formula for interpolation

(7)

X	30^{0}	32^{0}	35^{0}	38^{0}
tan x	0.5774	0.6249	0.7002	0.7813

- c) A second degree polynomial passes through the points (1,-1)(2,-1)(3,1)(4,5). Find the polynomial f(x), Also find f(1.2).
- 8 a) A river is 80 metre wide. The depth y in metres at a distance x metres from one

bank is given by the following table. Find approximately the area of cross section.

										(6)
X	0	10	20	30	40	50	60	70	80	
Y	0	5	8	10	15	12	7	3	1	

- b) Using Improved Euler method find y at x = 0.1 and x = 0.2 for the equation $y' = y \frac{2x}{y}, y(0) = 1. \tag{7}$
- c) Solve the initial value problem $y' + y \tan x = \sin 2x$, y(0) = 1 at x = 0.2 using Runge- Kutta method. (7)
- 9 a) Solve the following system of equations using Gauss elimination method.

$$10x + y + z = 6$$

 $x + 10y + z = 6$
 $x + y + 10z = 6$

(6)

b) Solve the system of equations using Gauss Seidel iteration method starting with the initial approximation x = y = z = 1. (7)

$$4x + 5z = 12.5$$

 $x + 6y + 2z = 18.5$
 $8x + 2y + z = -11.5$

c) The population of a town is as follows

Year (x)	1941	1951	1961	1971	1981	1991	
Population							(7)
in lakhs(y)	20	24	29	36	46	51	

Find the population increase during the period from 1946 to 1976