Reg No.:______ Name:_____

APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY

FOURTH SEMESTER B.TECH DEGREE EXAMINATION(S), DECEMBER 2019

Course Code: ME202 Course Name: ADVANCED MECHANICS OF SOLIDS

Max. Marks: 100 Duration: 3 Hours

PART A

Answer any three questions, each carries 10 marks

Databook is not permitted to use in the exam

1 a) Describe about the significance of stress invariants

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b) Given the stress matrix

$$[\sigma] = \begin{bmatrix} 20 & 10 & 10 \\ 10 & 20 & 10 \\ 10 & 10 & 20 \end{bmatrix} MPa$$

(a) Determine the principal stresses and the direction cosines associated with the maximum principal stress.

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- (b) Determine the maximum shear stress.
- (c) Determine the octahedral stresses 2
- 2 a) Write down the strain displacement relation in Cartesian Coordinate system 2
 - b) The displacement field for a body is given by $\mathbf{u} = [2y^2\mathbf{i} + 4yz\mathbf{j} + (3 + 35z^2)\mathbf{k}]10^{-2}$. Determine the strain tensor.
 - State the conditions under which the following is a possible system of strains $\varepsilon_{xx} = a + b(x^2 + y^2) + x^4 + y^4,$ $\varepsilon_{yy} = \alpha + \beta(x^2 + y^2) + x^4 + y^4, \quad \gamma_{xy} = A + Bxy(x^2 + y^2 c^2), \quad \gamma_{yz} = 0,$ $\gamma_{zx} = 0 \quad \text{and} \quad \varepsilon_{zz} = 0.$
- a) For steel the Young's Modulus is 207x10⁶ kPa and Rigidity Modulus is 80x10⁶ kPa. For the strain tensor at a point, determine the stress tensor

$$\begin{bmatrix} \varepsilon_{ij} \end{bmatrix} = \begin{bmatrix} 0.001 & 0 & -0.002 \\ 0 & -0.003 & 0.003 \\ -0.002 & 0.003 & 0 \end{bmatrix}$$
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- b) State and explain Saint Venant's principle for end effects
- c Write the constitutive relation for linear elastic isotropic material 2
- 4 a) Obtain the stress compatibility equation for plane stress problem in the presence 5 of body force
 - b) Show that $\phi = x^4 y + 4x^2 y^3 y^5$ is a valid stress function and compute the stress 5

tensor for this case assuming a state of plane strain with Poisson ratio $\nu=0.25$.

PART B

Answer any three questions, each carries 10 marks

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- 5 a) Derive the compatibility equation in terms of stress function φfor polar co-7 ordinate system
 - b) Write the equilibrium equation in polar coordinate system
- a) In a very thick cylinder with outer radius much larger than the inner radius a, subjected to an external pressure P_o and zero internal pressure, prove that the radial and tangential stress variations are $\sigma_r = P_0(1 \frac{a^2}{r^2})$ and $\sigma_\theta = P_0(1 + \frac{a^2}{r^2})$
- 7 a) Obtain the strain energy in terms of material properties for a shaft subjected to a 5 torque T.
 - b) For a given stress tensor at a point on a steel object with E= 207 x 10⁶ kPa and 5 G=80x10⁶ kPa, determine the value of strain energy density.

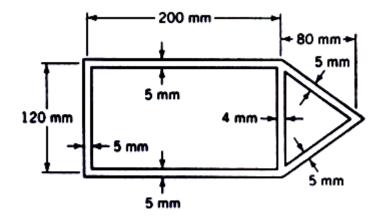
$$[\sigma] = \begin{bmatrix} 9 & 0 & 3 \\ 0 & -10 & 1 \\ 3 & 1 & 112 \end{bmatrix} x 10^3 \text{ kPa}$$

- 8 a) Explain about unsymmetrical bending of beams.
 - b) A beam symmetrical about y-z axis is subjected to a bending moment M, about 8 an arbitrary axis in the y-z plane. Obtain the equation for flexural stress.

PART C

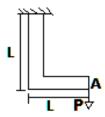
Answer any four questions, each carries 10 marks

- 9 a) Verify that function $\psi(x, y) = Axy$ is a Saint Venant's warping function, where 8 A is a constant. Find the general expression for slope of tangent at a point on the boundary curve of the bar with this warping function. Find out shape of the cross section and J integral.
 - b Explain about centre of twist.
- 10 a) Derive the governing equation and boundary condition for torsion of non circular 8 cross section in terms of Prandtl stress function.
 - b) What is torsional rigidity?
- 11 a) The aluminium (G=27GPa) hollow thin walled torsion member has dimensions as 10 shown below. Its length is 3m. If the member is subjected torque of 11KN-m, determine the maximum shear stress and angle of twist.



- 12 a) Based on the stress function approach, derive an expression for finding the 10 maximum shear stress on a shaft of elliptical cross section?
- 13 a) A frame is subjected to a load P as shown in figure. The length of each leg is L. 6

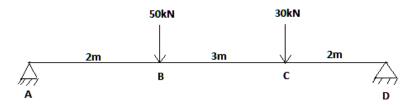
 The frame has a constant flexural rigidity EI. If the effect of axial load is neglected, find the deflection at point A due to applied load P?



b) State and explain Castigliano's first and second theorem

4 8

14 a)



Using the principle of virtual work, find out the reactions at A and D

b) Explain Maxwell theorem

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