

## Scheme of Valuation/Answer Key

(Scheme of evaluation (marks in brackets) and answers of problems/key)

**APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY**  
THIRD SEMESTER B.TECH DEGREE EXAMINATION, DECEMBER 2018

**Course Code: ME201**

**Course Name: MECHANICS OF SOLIDS (ME,MP,MA,MT,AU,PE,SF)**

Max. Marks: 100

Duration: 3 Hours

### PART A

*Answer any three full questions, each carries 10marks*

			Marks
1	a)	Derivation with figure	( 5)
	b)	<p><math>A_1 = 706.86 \text{ mm}^2</math>, <math>A_2 = 628.32 \text{ mm}^2</math> ..... 1M</p> <p><math>= 1 + 2 = \frac{P}{E} \left( \frac{L}{A} + \frac{L}{A} \right)</math> ..... 2M</p> <p>Substituting and solving <math>E = 3.31 \times 10^5 \text{ N/mm}^2</math> ..... 2 M</p>	( 5)
2		<p><math>s + b = b t L - s t L</math> ..... 2 M</p> <p>Solving <math>P = 20911.2 \text{ N}</math> ..... 4 M</p> <p>Stress in steel <math>= P/A_s = 14.2 \text{ N/mm}^2</math> ..... 2 M</p> <p>Stress in brass <math>= P/A_b = 42.6 \text{ N/mm}^2</math> ..... 2 M</p> <p style="text-align: center;">OR</p> <p><math>A_s = (502-252)/4</math>; <math>A_b = (252)/4</math> ..... 2 M</p> <p><math>S/E_s + b/E_b = b.t - s.t</math> ..... 2 M</p> <p><math>S \times A_s = b \times A_b</math> from this equation <math>S = 3 b</math> ..... 2 M</p> <p>Stress in steel, <math>s = 14.2 \text{ N/mm}^2</math> ..... 2 M</p> <p>Stress in brass, <math>b = 42.6 \text{ N/mm}^2</math> ..... 2 M</p>	(10)
3	a)	<p>Poissons ratio <math>= \text{Lateral strain} / \text{Longitudinal strain} = 0.25</math> ..... 1M</p> <p><math>E = 2G(1 + \mu)</math> ..... 1M</p> <p><math>G = 8.4 \times 10^4 \text{ N/mm}^2</math> ..... 1M</p> <p><math>E = 3K((1 - 2\mu))</math> ..... 1M</p> <p><math>K = 1.4 \times 10^5 \text{ N/mm}^2</math> ..... 1M</p>	(5)
	b)	True stress-strain curve with all salient points	(5)
4		$J_s = \frac{\pi}{3} 40^4 = 251327.41 \text{ mm}^4$	10

	$J_a = \frac{\pi}{3}(50^4 - 40^4) = 362264.9 \text{ mm}^4 \dots\dots\dots 2M$ $\frac{T}{G_s J_s} = \frac{T}{G_a J_a}$ $T_s = 2.05 T_a \dots\dots\dots 2 M$ <p>If stress in steel governs the resisting capacity</p> $\frac{T}{J_s} = \frac{q_s}{R} \dots\dots\dots 1M$ $T_s = 1507964.46 \text{ N.mm}$ $T_a = 735592.42 \text{ Nmm}$ $T = T_s + T_a = 2243556.86 \text{ N.mm} = 2243.56 \text{ Nm} \dots\dots\dots 2M$ <p>If stress in aluminium governs the resisting capacity</p> $\frac{T}{J_a} = \frac{q_a}{R}$ $T_a = 724529.8 \text{ N.mm}$ $T_s = 1485286.09 \text{ N.mm}$ $T = T_s + T_a = 2209815.89 \text{ N.mm} = 2209.82 \text{ Nm} \dots\dots\dots 2M$ <p>Stress in Steel governs the torque carrying capacity</p> $T = 2243.56 \text{ Nm} \dots\dots\dots 1 M$	
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**PART B**

*Answer any three full questions, each carries 10marks*

5	<p>Figure.....1M</p> <p>Reactions at supports <math>R_A = 65 \text{ kN}</math>, <math>R_B = 15 \text{ kN}</math>..... 2 M</p> <p>Shear force diagram..... 3 M</p> <p>Bending Moment diagram..... 4 M</p>	(10)
6	<p>a) Relation between load, shear force and bending moment</p>	(5)
	<p>b) Reactions at supports <math>R_A = - 4 \text{ kN}</math>, <math>R_B = 4 \text{ kN}</math>..... 1 M</p> <p>Shear force diagram..... 2 M</p> <p>Bending Moment diagram..... 2 M</p>	(5)
7	<p>Moment of Inertia of I section = <math>28490.72 \times 10^4 \text{ N/mm}^2</math> ..... 2M</p> <p>Distance of top layer from NA = 133.49 mm, Distance of bottom layer from NA = 166.51 mm ..... 2M</p> <p><math>M = WL/4 = 20 \text{ kN-m} = 20 \times 10^6 \text{ N.mm}</math> ..... 1 M</p> $\frac{\sigma}{y} = \frac{M}{I} \dots\dots\dots 1M$	(10)

	<p>Max tensile Stress, <math>\sigma_t = 11.68 \text{ N/mm}^2</math> ..... 2M</p> <p>Max compressive Stress, <math>\sigma_c = 9.37 \text{ N/mm}^2</math> ..... 2M</p>	
8	<p><math>I = 52160000 \text{ mm}^4</math> ..... 2M</p> <p>Shear stress distribution in top and bottom flange ..... 3 M</p> <p>Shear stress distribution in web ..... 3 M</p> <p>Shear stress distribution diagram..... 2M</p>	(10)
<b>PART C</b>		
<i>Answer any four full questions, each carries 10marks.</i>		
9	<p>Reactions at supports <math>R_A = 50 \text{ kN}</math>, <math>R_B = 50 \text{ kN}</math>..... 1 M</p> <p>Using Macaulays method,</p> <p><math>M_x = R_A \cdot x - 10(x-2)^2 + 10(x-7)^2</math> ..... 1 M</p> <p>Solving Constants of Integration, <math>C_1 = -454.166</math>, <math>C_2 = 0</math> ..... 3 M</p> <p>Slope equation and Deflection equation..... 2 M</p> <p>Deflection at mid span = 13.16 mm ..... 2 M</p> <p>Maximum deflection = 13.16mm..... 1 M</p>	(10)
10	<p>Reactions at supports <math>R_A = 3.333 \text{ kN}</math>, <math>R_B = 6.667 \text{ kN}</math>..... 1 M</p> <p>BM diagram.....2M</p> <p>Conjugate Beam.....2M</p> <p>Reactions at supports of conjugate beam <math>R_A^* = 17.77/EI \text{ kN}</math>,</p> <p><math>R_B^* = 22.22/EI \text{ kN}</math>.....1M</p> <p>Slope at left support = <math>4.44 \times 10^{-4} \text{ rad}</math> ..... 2M</p> <p>Deflection under load = <math>8.88 \times 10^{-4} \text{ m}</math> ..... 2M</p>	(10)
11	<p>Maximum principal stress <math>= \left(\frac{P}{2} + \frac{P}{2}\right) + \sqrt{\left(\frac{P}{2} - \frac{P}{2}\right)^2 + q^2}</math> ..... 2M</p> <p>Shear stress, <math>q = 72.11 \text{ N/mm}^2</math> .....2M</p> <p>Minimum Principal Stress <math>= \left(\frac{P}{2} + \frac{P}{2}\right) - \sqrt{\left(\frac{P}{2} - \frac{P}{2}\right)^2 + q^2} = -129.9 \text{ N/mm}^2</math>.....3M</p>	(10)

	<p>Maximum Shear stress = <math>\sqrt{\left(\frac{P - P}{2}\right)^2 + q^2} = 139.9 \text{ N/mm}^2, \dots\dots\dots 3\text{M}</math></p> <p><b>Note: Solutions obtained by using Mohr's circle should also be considered.</b></p>	
12	Derivation for Eulers crippling load	(10)
13	<p><math>I = \frac{b^4}{12} = 66.67 \times 10^6 \text{ mm}^4, \dots\dots\dots 1\text{M}</math></p> <p>At 20 mm below top fibre, <math>\sigma = \frac{M}{I} y = 23.99 \text{ N/mm}^2, \dots\dots\dots 2\text{M}</math></p> <p>Shear stress, <math>q = \frac{F \bar{y}}{I} = 1.08 \text{ N/mm}^2, \dots\dots\dots 3\text{M}</math></p> <p><math>P_x = 23.99 \text{ N/mm}^2, P_y = 0, q = 1.08 \text{ N/mm}^2</math></p> <p>Maximum principal stress = <math>\left(\frac{P + P}{2}\right) + \sqrt{\left(\frac{P - P}{2}\right)^2 + q^2} = 24.04 \text{ N/mm}^2 \dots\dots 2\text{M}</math></p> <p>Minimum Principal Stress = <math>\left(\frac{P + P}{2}\right) - \sqrt{\left(\frac{P - P}{2}\right)^2 + q^2} = -0.05 \text{ N/mm}^2 \dots\dots 2\text{M}</math></p>	(10)
14	<p>Rankine's load <math>P = \frac{c A}{[1 + a(l_e/k)^2]}, \dots\dots\dots 2\text{M}</math></p> <p>Radius of gyration <math>k = 62.5 \text{ mm} \dots\dots\dots 2\text{M}</math></p> <p><math>P = 1118.26 \text{ kN} \dots\dots\dots 2\text{M}</math></p> <p>Eulers formula <math>P = \frac{\pi^2 EI}{l^2} \dots\dots\dots 2\text{M}</math></p> <p><math>P = 1619.12 \text{ kN} \dots\dots\dots 2\text{M}</math></p>	(10)
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**Note: Evaluation is not strictly based on final answer and credit should be given to steps followed.**

**Chairman**