$\qquad$ Name: $\qquad$
APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY FIRST SEMESTER MCA DEGREE EXAMINATION, DECEMBER 2017

## Course Code: RLMCA105 <br> Course Name: APPLIED PROBABILITY AND STATISTICS

Max. Marks: 60
Duration: 3 Hours

## Statistical tables can be used. <br> PART A <br> Answer all questions, each carries 3 marks.

1 Why Arithmetic Mean is considered as best measure of central tendency?
State multiplication theorem of probability.

Derive mean of Geometric distribution.
Define mean and variance of a continuous random variable.
Define Normal distribution.
Define critical region and level of significance.
Define Stratified Sampling.
PART B
Answer six questions, one full question from each module and carries $\mathbf{6}$ marks.

## Module I

9 Find the missing frequencies of the following distribution. It is known that mean is 50 and total number of families is 100 .

| Expenditure | $0-20$ | $20-40$ | $40-60$ | $60-80$ | $80-100$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| No of families | 14 | $\ldots .$. | 27 | $\ldots \ldots$ | 15 |
| OR |  |  |  |  |  |

Scores of two batsmen A and B during a certain match are as follows.

| Batsman <br> A | 10 | 12 | 80 | 70 | 60 | 100 | 0 | 4 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Batsman <br> B | 8 | 9 | 7 | 10 | 5 | 9 | 10 | 8 |

Compare their variance and find who is more consistant.

## Module II

Probability that A solves the problem in Statistics is $\frac{2}{5}$. The probability that B
solves it is $\frac{3}{8}$. If they try independently find the probability that (i) both solve the problem (ii) none solves the problem (iii) at least one solves the problem.

## OR

12 The chance that doctor A will diagnose disease B correctly is $60 \%$. The chance that the patient will die by his treatment after correct diagnosis is $40 \%$ and the
chance of death by wrong diagnosis is $70 \%$. A patient of doctor A , who had disease B died. What is the chance that his disease was correctly diagnosed?

## Module III

Seven coins are tossed and number of heads are noted. The experiment is repeated 128 times and the following distribution is obtained. Fit a Binomial distribution to the following data.

| No of heads | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequencies | 7 | 6 | 19 | 35 | 30 | 23 | 7 | 1 |

## OR

If the probability that an individual suffers a bad reaction from an injection is 0.001 ,find the probability that out of 2000 individuals (i)at least 2 (ii ) at most 3 (iii ) none will suffer from a bad reaction.

## Module IV

A continuous random variable has PDF $f(x)=\left\{\begin{array}{c}k\left(1-x^{2}\right), 0<x<1 \\ 0 \text {,otherwise }\end{array}\right.$
(i) Find $k$ (ii) Find mean (iii) Find $\mathrm{P}(0.4<\mathrm{x}<0.6)$
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OR
Of a large group of men, $5 \%$ are under 60 inches in height and $40 \%$ are between 60 and 65 inches. Assuming normal distribution find mean and standard deviation.

## Module V

If 1-gallon of a certain paint covers on the average $513.3 \mathrm{ft}^{2}$ andstandard deviation of $31.5 \mathrm{ft}^{2}$, what is the probability that the mean area covered by a sample of 40 of these cans will be anywhere from $510.0 \mathrm{ft}^{2}$ to $520 \mathrm{ft}^{2}$ ?

## OR

Let the observed values of a random sample of size 9 from a normal distribution be $8.6,7.9,8.3,6.4,8.4,9.8,7.2,7.8,7.6$. Construct a $90 \%$ confidence interval for $\sigma^{2}$.

## Module VI

A filling machine is expected to fill 5 kg of powder into bags. A sample of 5 bags gave the following weights.4.7, 4.9, 5.0, 5.1, 5.2 Test whether the machine is working properly

OR
Intelligence test of two groups gave the following results:

|  | Mean | S.D | Number |
| :--- | :---: | :---: | :---: |
| Girls | 84 | 10 | 121 |
| Boys | 81 | 12 | 81 |

Is the difference in mean scores significant?

